

1.3 Explain - Solving Equations with Variables on Both Sides - Notes

Essential Question: How can you solve an equation that has variables on both sides?

Main Ideas/ Questions	Notes/Examples
<p>What You Will Learn</p>	<ul style="list-style-type: none"> <li>Solve linear equations that have variables on both sides</li> <li>Identify special solutions of linear equations</li> <li>Use linear equations to solve real-life problems</li> </ul>
<p>The Ultimate Goal</p>	<p>Goal: to get the variable you are solving for on one side of the equation by itself with a coefficient of positive one. Example: <math>x = 5</math></p>
<p>Solving Equations with Variables on Both Sides</p>	<p style="text-align: center;"><b>Steps to Solve Equations</b></p> <p><b>Step 1:</b> Use the distributive property to remove any grouping symbols.  <b>Step 2:</b> Simplify the expression on each side of the equation.  <b>Step 3:</b> Collect the variables on one side of the equation and the constant terms on the other side.  <b>Step 4:</b> Isolate the variable (add/subtract then multiply/divide).</p> <p>Practice: Solve each equation using inverses. Show all work.</p> <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>1. <math>12 - 3x = -6x</math> (CT)</p> <p style="margin-left: 20px;"><i>This side has no constants, so make it the VT side.</i></p> <math display="block">\begin{array}{r} 12 - 3x = -6x \\ +3x \quad +3x \\ \hline 12 = -3x \\ \div 3 \quad \div 3 \\ \hline -4 = x \end{array}</math> </div> <div style="width: 45%;"> <p>2. Check your solution to #1. (Plug -4 in for x:)</p> <math display="block">\begin{array}{l} 12 - 3(-4) = -6(-4) \\ 12 + 12 = 24 \\ 24 = 24 \checkmark \end{array}</math> </div> </div> <div style="display: flex; justify-content: space-between; margin-top: 20px;"> <div style="width: 45%;"> <p>3. <math>7 - 5z = 17 + 5z</math> (VT)</p> <math display="block">\begin{array}{r} 7 - 5z = 17 + 5z \\ -7 \quad -7 \\ \hline -5z = 10 + 5z \\ -5z \quad -5z \\ \hline -10z = 10 \\ \div -10 \quad \div -10 \\ \hline z = -1 \end{array}</math> </div> <div style="width: 45%;"> <p>4. Check your solution to #3. (Plug -1 in for z)</p> <math display="block">\begin{array}{l} 7 - 5(-1) = 17 + 5(-1) \\ 7 + 5 = 17 - 5 \\ 12 = 12 \checkmark \end{array}</math> </div> </div> <div style="display: flex; justify-content: space-between; margin-top: 20px;"> <div style="width: 45%;"> <p>5. <math>8 + 6x - 10x = 16 - 8x</math></p> <p><i>Combine like terms first!</i></p> <math display="block">\begin{array}{r} 8 - 4x = 16 - 8x \\ -8 \quad -8 \\ \hline -4x = 8 - 8x \\ +8x \quad +8x \\ \hline 4x = 8 \\ \div 4 \quad \div 4 \\ \hline x = 2 \end{array}</math> </div> <div style="width: 45%;"> <p>6. <math>9x - 12 = \frac{1}{4}(32x + 56)</math> ← Distribute first!</p> <math display="block">\begin{array}{r} 9x - 12 = 8x + 14 \\ +12 \quad +12 \\ \hline 9x = 8x + 26 \\ -8x \quad -8x \\ \hline x = 26 \end{array}</math> </div> </div>

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**Identifying Special Solutions of Linear Equations**

**Equations may have.....**

- 1 solution
- Infinitely Many Solutions – **identity** – an equation that is true for all values of the variable (Ex.  $-2 = -2$ )
- No Solution – an equation that is not true for any value of the variable (Ex.  $6 = 0$ )

**Practice:** Identify the number of solutions. Justify your answer by showing all work.

7.  $5x + 2(5x + 3) = 15x$

$$\begin{array}{r} \text{VT} \quad 5x + 10x + 6 = 15x \\ \text{CT} \quad 15x + 6 = 15x \quad \text{VT} \\ \hline -15x \quad -15x \\ \hline 6 \neq 0 \quad \text{FALSE!} \end{array}$$

The statement  $6 \neq 0$  is never true. So, the equation has NO solution.

**NO SOLUTION**

8.  $-2(4y + 1) = -8y - 2$

$$\begin{array}{r} \text{VT} \quad -8y - 2 = -8y - 2 \quad \text{CT} \\ \hline +8y \quad +8y \\ \hline -2 = -2 \quad \text{True!} \end{array}$$

The statement  $-2 = -2$  is always true. So, the equation is an identity and has infinitely many solutions.

**Using Linear Equations to Solving Real-Life Problems**

9. You and your friend drive toward each other. The equation  $50h = 5(38 - 9h)$  represents the number  $h$  of hours until you and your friend meet. When will you meet?

$$\begin{array}{r} \text{VT} \quad 50h = 5(38 - 9h) \\ \text{CT} \quad 50h = 190 - 45h \quad \text{CT} \\ \hline +45h \quad +45h \\ \hline 95h = 190 \quad h = 2 \end{array}$$

We will meet in 2 hours

10. A boat leaves New Orleans and travels upstream on the Mississippi River for 4 hours. The return trip takes only 2.8 hours because the boat travels 3 miles per hour faster downstream due to the current. How far does the boat travel upstream? Distance = (rate)(time)

$x =$  speed of boat traveling upstream (rate)

Distance upstream = Distance downstream

$$\begin{array}{r} 4x = 2.8(x + 3) \\ \text{VT} \quad 4x = 2.8x + 8.4 \quad \text{CT} \\ \hline -2.8x \quad -2.8x \\ \hline 1.2x = 8.4 \\ \hline \frac{1.2x}{1.2} = \frac{8.4}{1.2} \quad x = 7 \text{ miles per hour} \end{array}$$

So, the distance is  $7(4) = 28$  miles

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Solving Equations with Variables on Both Sides	<p style="text-align: center;"><b>Steps to Solve Equations</b></p> <p><b>Step 1:</b> Use the distributive property to remove any grouping symbols.  <b>Step 2:</b> Simplify the expression on each side of the equation.  <b>Step 3:</b> Collect the variables on one side of the equation and the constant terms on the other side.  <b>Step 4:</b> Isolate the variable (add/subtract then multiply/divide).</p>
	<p><b>Practice:</b> Solve each equation using inverses. Show all work.</p> <p>1. <math>12 - 3x = -6x</math> <span style="float: right;">2. Check your solution to #1.</span></p> <p>3. <math>7 - 5z = 17 + 5z</math> <span style="float: right;">4. Check your solution to #3.</span></p> <p>5. <math>8 + 6x - 10x = 16 - 8x</math> <span style="float: right;">6. <math>9x - 12 = \frac{1}{4}(32x + 56)</math></span></p>

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8.  $-2(4y + 1) = -8y - 2$

The statement \_\_\_\_\_ is never true. So, the equation has \_\_\_\_\_ solution.

The statement \_\_\_\_\_ is always true. So, the equation is an \_\_\_\_\_ and has \_\_\_\_\_ solutions.

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